

# Effects of Perforated Partition Plate on Mixing Characteristics of Horizontal Stirred Vessel

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To reduce backmixing in the flow-type horizontal stirred vessel, a perforated partition plate was attached and the effects of shape of plate on the mixing characteristics were studied under various operating conditions. Results were analyzed in terms of mixing models to evaluate the extent of preventing backmixing. It enabled us to estimate the extent of back flow at the perforated partition plate from power consumption.

## SCOPE

The purpose of the present study is to clarify the effects of the shape of perforated plate attached inside a flow-type horizontal stirred vessel under various operating conditions upon reducing liquid backmixing.

Kirk and Othmer (1951) and Ullmann (1928) showed a horizontal stirred vessel as a gas-liquid contactor for production of sodium formate from carbon monoxide and aqueous caustic soda. Ganz et al. (1958) carried out absorption experiments with various gas-liquid systems and observed that the horizontal stirred vessel equipped with a deformed circular plate as an impeller had high absorption capability. Recent studies on horizontal stirred vessels include those carried out by Ando et al. (1972), Misaka (1967), Sasaki (1971), Takeuchi et al. (1976), and Tamaki et al. (1974, 1975). In these studies, effects of the operating conditions, types of impeller, and flow behavior on the gas-liquid contact in the vessel have been examined. Power consumption was also examined by Ando et al. (1971a, 1978),

Misaka (1967), and Tamaki and Ito (1973). In the foregoing studies, however, no consideration was given to the use of a partition plate as a means to reduce backmixing.

Fukuda et al. (1976) studied desorption of hydrogen cyanide from waste water using a commercial horizontal stirred vessel (1 m in diameter and 2 m in length) in a gas-liquid flow system. The apparatus used had a large contact area for its volume, and it was possible to control flow rates of gas and liquid separately. Even though the apparatus was found to desorb hydrogen cyanide effectively, they suggested the necessity of improving the liquid mixing characteristics since the liquid mixing under the conditions employed was close to complete mixing. Ando et al. (1971b, 1974) studied the effects of various operating conditions upon mixing time and residence time distribution, using a vessel without a perforated partition plate. No other report has been published to the present author's knowledge, on the mixing characteristics of a horizontal stirred vessel.

## CONCLUSIONS AND SIGNIFICANCE

Liquid mixing in the present apparatus would be approximated adequately by a backmixing model consisting of completely mixed cells separated by a perforated partition plate and impellers. Based on this model, an equation  $u_p' = Q_p - u/2$  was found to hold for the back-flow rate at the plate ( $u_p'$ ), the liquid flow rate ( $u$ ) and the rate of exchange between two cells separated by the plate ( $Q_p$ ). The relation holds for a wide range

of operating conditions, perforated plate shapes, and apparatus of various size. The values of  $Q_p$  were estimated from the power consumption.

Further, the partition plates composed of two parallel, thin, perforated plates were as good as or better than that of the single thick plate with long flow path.

A horizontal stirred vessel effectively mixes gas and liquid with rotating impeller, installed on a horizontal shaft, at the gas-liquid interface.

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Most of the research reports on horizontal stirred vessels are concerned with the relationships among the gas-liquid contact, power consumption, types of impeller, and operating conditions (Ando et al., 1971a, 1972, 1978; Ganz, 1958; Misaka, 1967; Sasaki, 1971; Takeuchi et al., 1976; Tamaki and Ito, 1973; and Tamaki et al., 1974, 1975). Few reports have been published on mixing characteristics of horizontal stirred vessels.

Ando et al. (1971b, 1978) studied the relationship among operating conditions, mixing time of liquid, and residence time

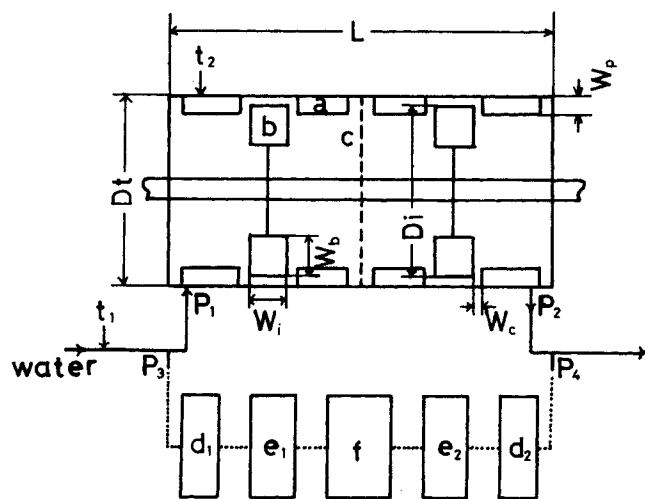


Figure 1. Schematic of the apparatus.

distribution. When a horizontal stirred vessel, used in a flow system, is operated under the condition that mean residence time of liquid is relatively long, liquid mixing in the vessel approaches complete mixing. Hence, the mixing characteristics must be improved for efficient mass transfer between gas and liquid (Fukuda et al., 1976).

In the present study, we attached a perforated plate inside a horizontal stirred vessel to reduce backmixing of liquid in a flow system operation and, using various size of apparatus, examined the effects of plate shape and operating conditions on the partition effect. A model for mixing in a horizontal stirred vessel equipped with a perforated partition plate was presented. A procedure to estimate the liquid mixing characteristics of the apparatus based on this model was given.

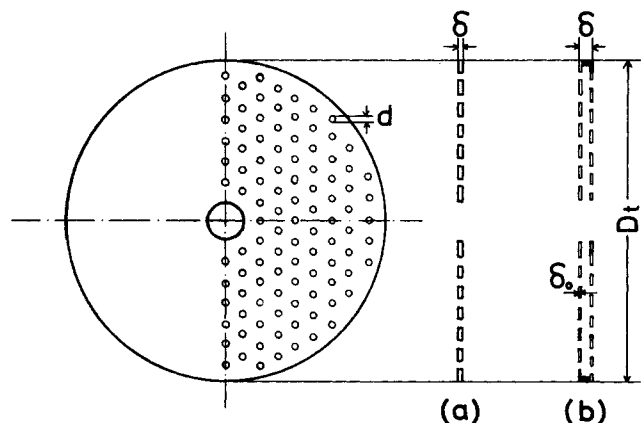


Figure 2. Perforated copper, polyethylene and acrylic plates in an equilateral triangle arrangement.

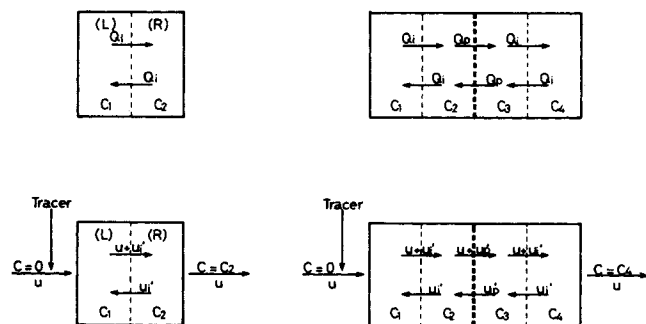


Figure 3. Mixing models for horizontal stirred vessels.

## APPARATUS AND EXPERIMENTAL PROCEDURE

A schematic diagram of the apparatus used is shown in Figure 1. Two geometrically similar cylinders (0.15 and 0.23 m in diameter) equipped with four baffle plates at the top, bottom, left and right of the inside wall, were used as the horizontal vessel. In the center of the vessel was attached a perforated partition plate. In the center of the shaft of each cell, separated by the plate, was installed a four-blade turbine impeller. The shapes and principal dimensions of the stirred vessel, impeller, and baffle plate are shown in the diagram; they are practically the same as those used by Ando et al. (1974). Copper, polyethylene and acrylic plates, with thickness  $1 \times 10^{-4}$  to  $3 \times 10^{-3}$  m, were perforated in an equilateral triangle arrangement as shown in Figure 2. Number of holes was either 12, 75, 192, or 300. Diameters of hole ranged between  $1.4 \times 10^{-3}$  and  $1 \times 10^{-2}$  m. The partition plates composed of two perforated thin-plates as shown in Figure 2(b) were also examined. They were arranged parallel at a short distance with their hole positions slightly staggered. Open area ratio  $\gamma$ , hole number  $m$ , hole diameter  $d$  and vessel diameter  $D_t$  are related by an equation  $\gamma = m \cdot d^2/D_t^2$ . Throughout this study, a flow system was adopted only for the liquid, and the mixing characteristics of the liquid were determined by delta response method. A potassium chloride solution was injected at  $p_5$  as a tracer. The tracer concentrations at  $p_3$  of the inlet and  $p_4$  of the outlet tube were followed by means of electric resistance of the liquid using bridges with two platinum electrodes and recorded simultaneously on a two-pen recorder.

The horizontal stirred vessel with baffle plate has the large absorption capability, when the vessel is approximately half filled with liquid (Ando et al., 1972). The present work was conducted in the liquid ratio  $\epsilon$  (ratio of volume of liquid to volume of vessel) ranging from 0.4 to 0.6.

## MIXING MODELS AND BACK FLOW RATE AT PERFORATED PARTITION PLATE $u'_p$

### Mixing Models

The mixing models proposed by Ando et al. (1974) for horizontal stirred vessels with an impeller, but without a perforated partition plate, are shown in Figure 3(a) and (b). For batch vessel, mixing is controlled by liquid exchange rate  $Q_i$  between the two completely mixed cells separated by an impeller, as shown in Figure 3(a). On the other hand, a model consisting of two completely mixed cells with back flow rate  $u'_i$ , Figure 3(b) describes mixing in the flow system.

For the present case where the plate is attached between two impellers, two foregoing models connected in series [Figures 3(c) and (d)] appear appropriate. That is, if a treatment similar to that of Ando et al. (1974) is applicable here, the liquid mixing in the present flow system should be adequately described by a model consisting of four completely mixed cells separated by two impellers and a perforated plate, with back flow rate  $u'_i$  in the vicinity of each impeller and back flow rate  $u'_p$  at the plate. Thus, the mixing characteristics of the apparatus are given by Eqs. 1 and 2:

$$\beta_p \equiv u'_p/u \quad (1)$$

$$\beta_i \equiv u'_i/u \quad (2)$$

where  $\beta_p$  means the partition effect of the perforated plate and  $\beta_i$  the mixing effect of a vessel without the plate. According to the previous study (Ando et al., 1974),  $\beta_i$  is estimated from power consumption.

Based on the back mixing model of Figure 3(d), the material balance is given by Eqs. 3 to 6. When the tracer is injected at time  $\theta = 0$ , the concentration at time  $\theta$  of the tracer for each cell are  $C_1$ ,  $C_2$ ,  $C_3$  and  $C_4$ :

First cell:

$$\frac{V}{4} \frac{dC_1}{d\theta} = C_2 u'_i - C_1(u + u'_i) \quad (3)$$

Second cell:

$$\frac{V}{4} \frac{dC_2}{d\theta} = C_3 u'_p - C_2(u + u'_i + u'_p) + C_1(u + u'_i) \quad (4)$$

Third cell:

$$\frac{V}{4} \frac{dC_3}{d\theta} = C_4 u'_i - C_3(u + u'_i + u'_p) + C_2(u + u'_p) \quad (5)$$

Fourth cell:

$$\frac{V}{4} \frac{dC_4}{d\theta} = -C_4(u + u'_i) + C_3(u + u'_i) \quad (6)$$

Since  $C_1 = 4$  and  $C_2 = C_3 = C_4 = 0$  at  $\theta = 0$ , the residence time distribution function  $E(\phi)$  is given by Eq. 7:

$E(\phi) =$

$$16(1 + \beta_i)^2 \sqrt{\frac{1 + \beta_p}{\beta_p}} \left\{ \frac{\exp(D + B)\phi}{B^2 + 2(\sqrt{\beta_p}(1 + \beta_p) - \beta_p)B} + \frac{\exp(D - B)\phi}{B^2 - 2(\sqrt{\beta_p}(1 + \beta_p) - \beta_p)B} - \frac{\exp(C + A)\phi}{A^2 - 2(\sqrt{\beta_p}(1 + \beta_p) + \beta_p)A} - \frac{\exp(C - A)\phi}{A^2 + 2(\sqrt{\beta_p}(1 + \beta_p) + \beta_p)A} \right\} \quad (7)$$

where

$$A = 2\sqrt{4\beta_i(1 + \beta_i) + 2\beta_p(1 + \beta_p) - \beta_p(1 - 2\sqrt{\beta_p}(1 + \beta_p))}$$

$$B = 2\sqrt{4\beta_i(1 + \beta_i) + 2\beta_p(1 + \beta_p) - \beta_p(1 + 2\sqrt{\beta_p}(1 + \beta_p))}$$

$$C = 2[-2(1 + \beta_i) - \beta_p - \sqrt{\beta_p}(1 + \beta_p)]$$

$$D = 2[-2(1 + \beta_i) - \beta_p + \sqrt{\beta_p}(1 + \beta_p)]$$

and where  $\phi(\equiv \theta/\theta_T)$ ,  $\theta_T(\equiv V_1/u)$  and  $V_1$  are dimensionless residence time, mean residence time and total volume of liquid in the vessel, respectively.

#### Calculation of Back Flow Ratio at Perforated Partition Plate $\beta_p(\equiv u'_p/u)$

Figure 4 shows an example of response curve. Curve A illustrates a concentration change on the inlet side, and curve B that on the outlet side. The starting time ( $\theta = 0$ ) is taken when the tracer concentration on the inlet side begins to tail.  $\theta_s$  in Figure 4 means the difference between the starting position of curve A and that of B.  $\theta_{max}$  is the time corresponding to the maximum of the response curve. The time needed for the liquid to pass through the tube sections ( $p_3$ -vessel,  $p_4$ -vessel in Figure 4) is negligible compared to  $\theta_{max}$ .

Circles in Figure 4 are the values calculated from Eq. 7, using  $\beta_p = 0.9$  and  $\beta_i = 6$ . Figure 4 indicates that the experimental values agree quite well with the calculated ones. Under other operating conditions, agreement between experimental and calculated values was also satisfactory. Therefore, in the following analysis, back flow ratio  $\beta_p(\equiv u'_p/u)$  and back flow rate  $u'_p$  at the plate were determined using experimental dimensionless time  $\phi_{max}(\equiv \theta_{max}/\theta_T)$  and  $\beta_p/\beta_i - \phi_{max}$  relationship of Figure 5. The values for  $\beta_i$  were obtained from Eq. 24, as will be discussed later.

#### Relation between Back Flow $u'_p$ at Perforated Partition Plate and Liquid Flow $u$

Figure 6 shows the relationship between experimental back flow rate  $u'_p$  at the plate and liquid flow rate  $u$ . The rate  $u'_p$  decreases with an increase in  $u$ , giving a slope of approximately  $-1/2$ . At a constant liquid flow rate,  $u'_p$  increases as the speed of the impeller rotation  $n$ , the liquid-vessel volume ratio  $\epsilon$ , and the open area ratio of the plate  $\gamma$  increase. On the other hand,  $u'_p$  decreases as the thickness of the perforated plate  $\delta$  increases. A straight line with a slope of  $-1/2$  is drawn for each set of data and its intercept at  $u = 0$  is taken as  $u'_{p0}$ :

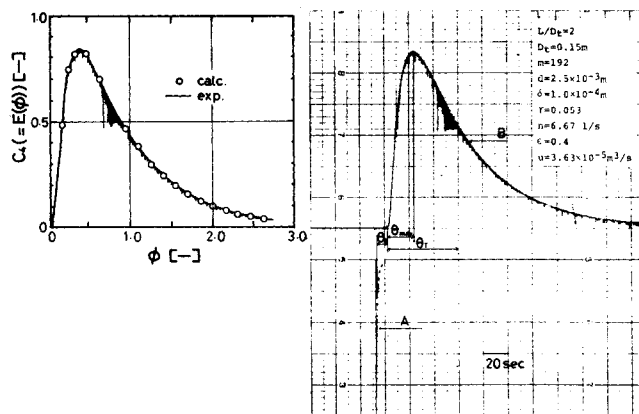


Figure 4. Example of response curve.

$$u'_p = u'_{p0} - \frac{1}{2}u \quad (8)$$

The plots of  $u'_p/u'_{p0}$  against  $u/u'_{p0}$  are shown in Figure 7. Hence, Eq. 8 holds for a wide range of operating conditions, perforated plate shapes, and apparatus scales.

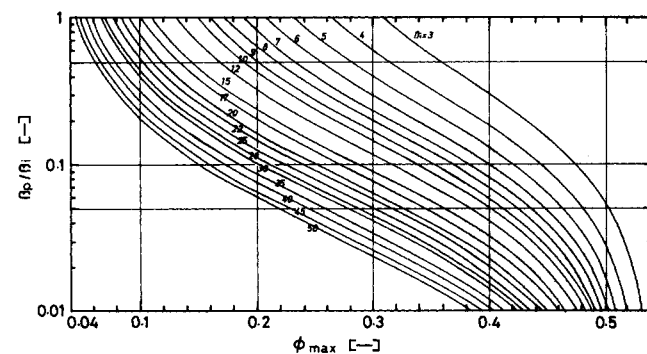


Figure 5. Relationship of  $\beta_i$  and  $\beta_p/\beta_i - \phi_{max}$ .

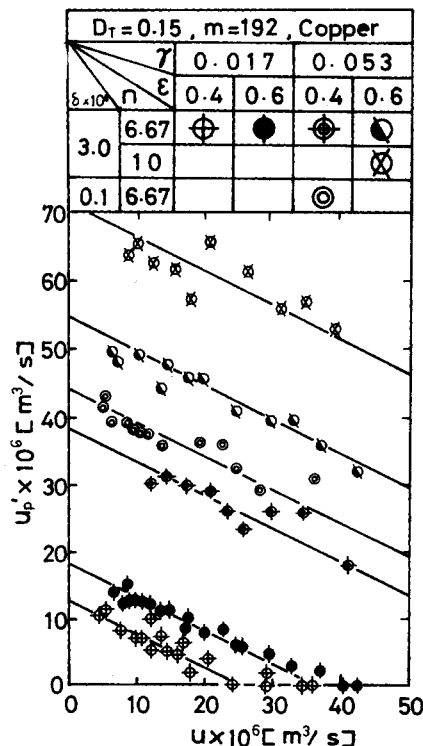


Figure 6. Relationship between experimental back flow rate and liquid flow rate.

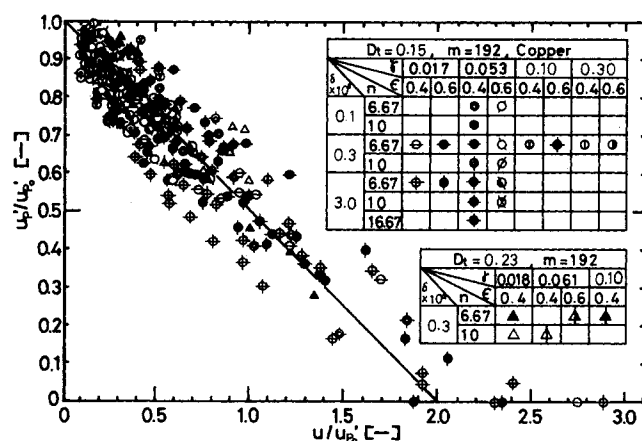


Figure 7. Plots of  $u_p/u_{p0}$  against  $u/u_{p0}$ .

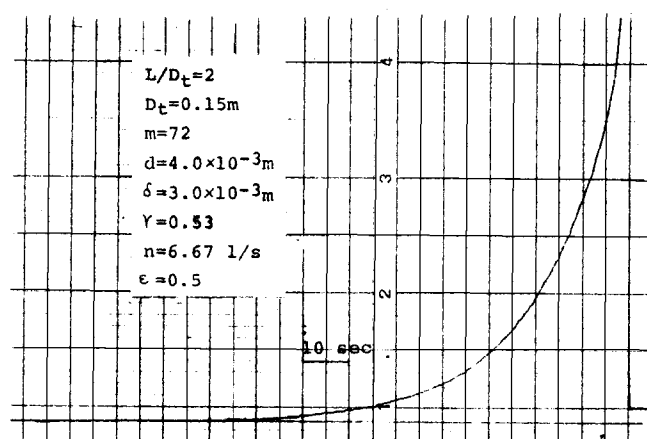


Figure 8. Relationship between pen position and time.

## EXCHANGE RATE RATIO $Q_p/Q_i$ OF BATCH OPERATION

### Measurements of Exchange Rate Ratio $Q_p/Q_i$

The same method as described in the previous report (Ando et al., 1971b) was employed to measure the mixing time of batch vessel. Namely, two pairs of platinum electrode were installed at  $p_1$  and  $p_2$ , i.e. two bottom positions, Figure 1. The electric resistance of liquid at the electrodes was used as the resistance of bridge circuit. Solution of potassium chloride was injected from above  $p_1$  as a tracer, and its concentration change with time was followed by measuring electric resistance. Under the experimental conditions employed, the response of recording pen changed proportionately to the difference in tracer concentrations between the electrodes.

Figure 8 illustrates the relationship between the pen position and time. The pen positions relative to that after a sufficiently long period were measured at each time  $\theta$ . The displacement, or the concentration difference between  $p_1$  and  $p_2$ , ( $C_1 - C_4$ ), decreases exponentially with time and was approximated by the following equation:

$$C_1 - C_4 = K \exp(-\theta/\tau) \quad (9)$$

In the present study, mixing time  $\theta_M$  is defined as  $4\tau$  corresponding to 98% equilibration.

The exponential relationship of Eq. 9 may be interpreted based on the mixing model of Figure 3(c). The model presupposes that the vessel consists of completely mixed cells separated by the impellers and the plate and that the liquid exchange rate across the two adjacent cells controls the over-all mixing. If the exchange rate at the impeller and that at the plate are designated as  $Q_i$  and  $Q_p$ , respectively, the material balance for each cell as to tracer concentration is expressed as follows:

First cell:

$$\frac{V}{4} \frac{dC_1}{d\theta} = Q_i(C_2 - C_1) \quad (10)$$

Second cell:

$$\frac{V}{4} \frac{dC_2}{d\theta} = Q_i(C_1 - C_2) + Q_p(C_3 - C_2) \quad (11)$$

Third cell:

$$\frac{V}{4} \frac{dC_3}{d\theta} = Q_p(C_2 - C_3) + Q_i(C_4 - C_3) \quad (12)$$

Fourth cell:

$$\frac{V}{4} \frac{dC_4}{d\theta} = Q_i(C_3 - C_4) \quad (13)$$

Since  $C_1 = 1$  and  $C_2 = C_3 = C_4 = 0$  at  $\theta = 0$ , the difference in concentration between cell 1 and cell 4,  $\Delta C (= C_1 - C_4)$ , is obtained as follows:

$$\Delta C = \frac{Q_i^2}{2(Q_i^2 + Q_p^2 - Q_p\sqrt{Q_i^2 + Q_p^2})} \exp \left\{ \frac{-4(Q_i + Q_p - \sqrt{Q_i^2 + Q_p^2})}{V_1} \cdot \theta \right\} + \frac{Q_i^2}{2(Q_i^2 + Q_p^2 + Q_p\sqrt{Q_i^2 + Q_p^2})} \exp \left\{ \frac{-4(Q_i + Q_p + \sqrt{Q_i^2 + Q_p^2})}{V_1} \cdot \theta \right\} \quad (14)$$

If  $\theta$  is sufficiently large, the first term of Eq. 14 becomes large compared with the second term. Thus, in the region where the second term is negligible, mixing time  $\theta_M$  and relaxation time  $\tau$  would be approximated by the following equation:

$$\theta_M \equiv 4\tau = \frac{V_1}{Q_i + Q_p - \sqrt{Q_i^2 + Q_p^2}} \quad (15)$$

In Table 1 are shown the relationship between  $\Delta C$  of Eq. 14 and dimensionless time  $\psi (= \theta/\theta_M)$  and that between the first term of Eq. 14 and  $\psi$ . Table 1 shows evidently that the second term of

TABLE 1. RELATION BETWEEN  $\Delta C$  CALCULATED FROM EQUATION (14) AND FIRST TERM OF EQUATION (14) FOR VARIOUS  $\psi$  AND  $Q_p/Q_i$

$\psi$ ( $\equiv \theta/\theta_M$ )	$Q_p/Q_i = 1.0$		$Q_p/Q_i = 0.3$		$Q_p/Q_i = 0.1$	
	$\Delta C$	1st term	$\Delta C$	1st term	$\Delta C$	1st term
0.01	0.9361	0.8201	0.8655	0.6184	0.7138	0.5282
0.02	0.8798	0.7879	0.7655	0.5942	0.5840	0.5075
0.05	0.7445	0.6988	0.5841	0.5270	0.4555	0.4501
0.1	0.5864	0.5722	0.4406	0.4315	0.3636	0.3685
0.2	0.3849	0.3835	0.2895	0.2892	0.2470	0.2470
0.5	0.1155	0.1155	0.0871	0.0871	0.0744	0.0744
1.0	0.0156	0.0156	0.0118	0.0118	0.0101	0.0101

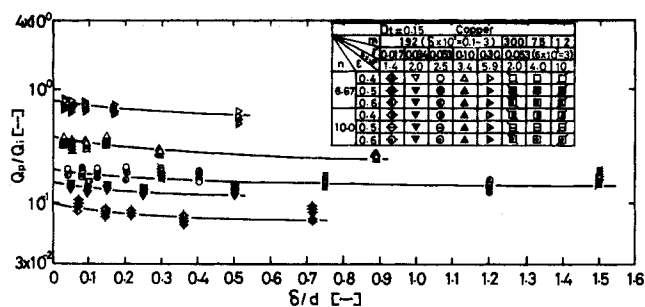


Figure 9. Ratio of experimentally determined exchange rate vs. ratio of the thickness to the hole diameter of perforated partition plate.

Eq. 14 will be neglected in the region where  $\psi > 0.1$ .

Analogously, mixing time  $\theta_{M1}$ , of the single-impeller model shown in Figure 3(a), ( $L/D_t = 1.0$ ) is expressed as follows:

$$\theta_{M1} = \frac{V_1/2}{Q_i} \quad (16)$$

If exchange rate  $Q_i$  at the impeller is assumed to remain unaffected by the presence of a perforated partition plate, that is, if  $Q_i$  of Figure 3(a) is equal to  $Q_i$  of Figure 3(c), the following equation is obtained from Eqs. 15 and 16.

$$\frac{Q_p}{Q_i} = \frac{2\theta_{M1}(\theta_M - \theta_{M1})}{\theta_M(\theta_M - 2\theta_{M1})} \quad (17)$$

Eq. 17 means that the exchange rate ratio  $Q_p/Q_i$  can be determined experimentally by measuring mixing time  $\theta_M$  of a vessel with the perforated partition plate, Figure 3(c), and mixing time  $\theta_{M1}$  of a cell equipped only with an impeller, Figure 3(a).

#### Relationship between Exchange Rate Ratio $Q_p/Q_i$ and Operating Conditions and Shape of Perforated Partition Plate

The relationship between experimentally determined exchange rate ratio  $Q_p/Q_i$  and the ratio of thickness to hole diameter  $\delta/d$  of perforated partition plate is shown in Figure 9. For the same plate,  $Q_p/Q_i$  stays nearly even if operating conditions ( $n, \epsilon$ ) were changed. The relationship between  $Q_p/Q_i$  and  $\delta/d$  does not change significantly with the plate shapes ( $\delta, d$  and  $m$ ), as long as the open area ratio  $\gamma$  remains constant. Thus, at a constant open area ratio,  $Q_p/Q_i$  decreases with an increase in  $\delta/d$  and reaches a constant value regardless of operating conditions. Further, if  $\delta/d$  is kept constant,  $Q_p/Q_i$  increases with an increase in  $\gamma$ . The dependence of  $Q_p/Q_i$  on  $\gamma$  and on  $\delta/d$  was obtained experimentally as shown in Figure 10. The solid line drawn follows the following equation:

$$\frac{Q_p}{Q_i} = \frac{2\gamma^{0.73}}{1 + 0.4(\delta/d)^{0.5}} \quad (18)$$

where  $0.017 < \gamma < 0.30$  and  $0.03 < \delta/d < 2.15$ . Experimental results obtained with apparatus of various size are now correlated in terms of Eq. 18 with an accuracy of  $\pm 20\%$ .

Haug (1971) pointed out that, with a multistage stirred-type counterflow contactor, the wettability and interfacial tension affect the partition effect. For this reason, we examined the partition effects of perforated plates made of polyethylene and acrylic resins. A part of the results are shown in Figure 10. No significant difference is observed between these perforated plates and that made of copper.

Figure 10 also shows a part of the exchange rate ratio  $Q_p/Q_i$  measured with a parallel set of two perforated thin-plates, Figure 2(b). The measured values are in the vicinity of the broken line and indicate a deviation of  $\sim 20\%$  from the empirical equation (Eq. 18) derived with single perforated plate, Figure 2(a).  $Q_p/Q_i$  of the parallel set of two perforated plates is affected by thickness  $\delta_0$  of the perforated plate used; even if the total thickness  $\delta$  is kept constant,  $Q_p/Q_i$  decreases with an increase in  $\delta_0$ .

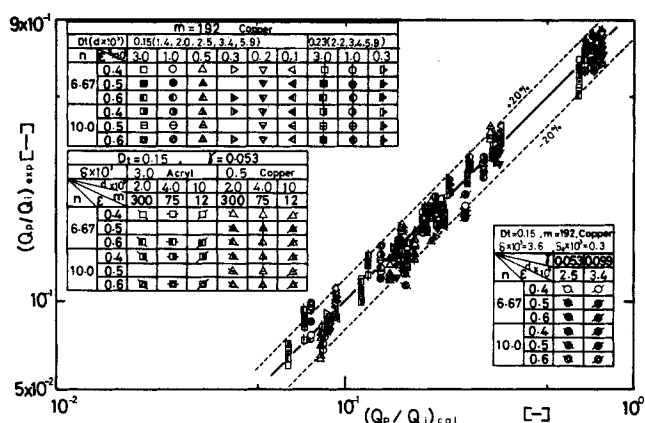


Figure 10. Partition effects of perforated plates made of copper and acrylic resin.

However, if  $\delta_0/d$  is equal to or less than 0.1,  $Q_p/Q_i$  follows Eq. 18. Namely, the partition effect of the parallel set of two perforated thin-plates is as good as or better than that of single perforated plate of equal thickness  $\delta$ . Therefore, if the thickness of a single perforated plate becomes excessively large as a result of scale-up under the geometrical similarity rule, use of partition plate composed of two perforated thin-plates is advantageous.

#### RELATION BETWEEN BACK FLOW $u'_p$ AND EXCHANGE RATE $Q_p$

As is evident from mixing models, Figure 3(c) and (d), the back flow  $u'_{p0}$ , obtainable by substituting zero for  $u$  in Eq. 8, is equal to the exchange rate  $Q_p$  of batch process. Therefore, what has been found with the exchange rate  $Q_p$  should be applicable to  $u'_{p0}$  in Eq. 8 as well. If one put  $Q_p$  in place of  $u'_{p0}$ , Eq. 8 becomes:

$$\frac{u'_p}{u} (\equiv \beta_p) = \frac{Q_p}{u} - \frac{1}{2} \quad (19)$$

From Eqs. 18 and 19, one obtains:

$$\frac{u'_p}{u} (\equiv \beta_p) = \frac{2\gamma^{0.73}}{1 + 0.4(\delta/d)^{0.5}} \cdot \frac{Q_i}{u} - \frac{1}{2} \quad (20)$$

According to the previous report (Ando et al., 1974) on the mixing characteristics of horizontal stirred vessel without a perforated plate,  $Q_i/u$  in Eq. 20 is given by the Eqs. 21 and 22:

$$\frac{u'_i}{u} (\equiv \beta_i) = K \cdot \frac{\theta_{T1}}{\theta_{M1}} \left( = K \cdot \frac{Q_i}{u} \right) \quad (21)$$

$$K = 0.85 \text{ and } \beta_i > 1.5$$

$$\frac{1}{n\theta_M} \frac{L}{D_t} = 2.3 \times 10^{-2} \left( \frac{N_p}{\epsilon} \right)^{0.7} \quad (22)$$

In Eqs.,  $\theta_{M1}$  and  $\theta_{T1}$  denote mixing time and mean residence time of a vessel without a perforated plate, respectively, and  $N_p$  means the power number. The value of  $K$  in Eq. 21, has been determined experimentally, using a relationship that  $u'_i = KQ_i$ , regardless of the magnitude of  $u$ . If  $Q_i/u$  is sufficiently small, however, the effect of  $u$  on back flow  $u'_i$  cannot be neglected. Thus, Eq. 21 holds only when  $\beta_i > 1.5$  or  $Q_i/u > 2$ . The same argument on Eq. 19 gives the effect of flow rate  $u$  on the relationship between back flow  $u'_i$  and exchange rate  $Q_i$  in the form of Eq. 23:

$$\frac{u'_i}{u} (\equiv \beta_i) = \frac{Q_i}{u} - \frac{1}{2} \quad (23)$$

Eq. 23 holds for the data of the previous report even if  $Q_i/u (= \theta_{T1}/\theta_{M1})$  is small. Thus, in the present study, the values of  $\beta_i$  were calculated according to the following equation obtained from Eqs. 22 and 23.

$$\frac{u'_i}{u} (\equiv \beta_i) = 2.3 \times 10^{-2} \frac{n\theta_T}{(L/D_t)} \left( \frac{N_p}{\epsilon} \right)^{0.7} - \frac{1}{2} \quad (24)$$

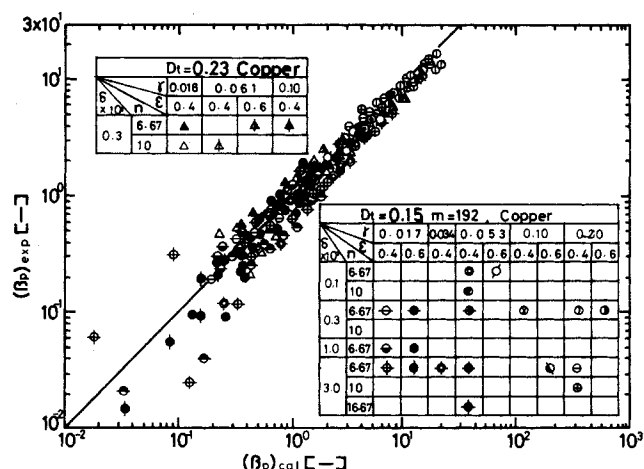


Figure 11. Experimentally obtained back flow ratio.

Figure 11 shows plots of experimentally obtained back flow ratio  $\beta_p$  at the perforated partition plate against the right-hand side of Eq. 20. A good correlation exists for a wide range of operating conditions. Essentially the same correlation was obtained with the partition plate composed of two perforated thin-plates.

The results obtained above clearly indicate that the back flow  $\beta_p$  at the perforated partition plate of the present apparatus is estimated from power number  $N_p$  and Eq. 20.

## CONCLUSIONS

For the purpose of improving the liquid mixing characteristics of flow-type horizontal stirred vessel, perforated partition plate was attached to the inside of the vessel. The effects of the plate shape (hole diameter  $d$ , open area ratio  $\gamma$ , thickness  $\delta$ ) and operating conditions (flow rate  $u$ , rotational speed of impeller  $n$ , ratio of volume to vessel volume  $\epsilon$ ) on the partition efficiency were studied using apparatus of various size. Results were analyzed in terms of several mixing models, and the effect of the perforated partition plate on backmixing reduction was evaluated.

The mixing of liquids inside the present apparatus would be approximated adequately by a backmixing model consisting of completely mixed cells separated by the partition plate and impellers. From the mixing models, a relationship ( $u'_p = Q_p - u/2$ ) was derived among the back flow  $u'_p$  at the partition plate, the exchange rate  $Q_p$  at the partition plate of a batch vessel, and the liquid flow rate  $u$ . The relationship was subsequently confirmed by experiments. The dependence of the plate shape on the exchange rate  $Q_p$  is calculated in Eq. 18.

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## NOTATION

$c$	= concentration
$c_j$	= concentration of KCl solution in $j$ th cell
$D_i$	= diameter of impeller
$D_t$	= diameter of horizontal stirred vessel
$d$	= diameter of hole in perforated plate
$E(\phi)$	= distribution function for residence time
$g$	= acceleration of gravity
$L$	= length of horizontal stirred vessel
$m$	= number of holes in perforated plate
$n$	= rotational speed of impeller
$N_{Fr}$	= Froude number ( $=n^2 D_i/g$ )
$N_p$	= Power number ( $=P/\rho n^3 D_i^5$ )
$P$	= power consumption
$Q_i$	= exchange rate of liquid between 1st and 2nd cell or 3rd and 4th cell (at impeller)

$Q_p$	= exchange rate of liquid between 2nd and 3rd cell (at partition plate)
$u$	= net volumetric flow rate
$u'_i$	= back flow rate of liquid between 1st and 2nd cell or 3rd and 4th cell (at impeller)
$u'_p$	= back flow rate of liquid between 2nd and 3rd cell (at partition plate)
$u'_{p0}$	= extrapolated value of $u'_p$ obtained by putting $u = 0$ in Eq. 8
$V$	= volume of horizontal stirred vessel
$V_1$	= volume of liquid in horizontal stirred vessel

## Greek Letters

$\beta_i$	= back flow ratio at impeller ( $=u'_i/u$ )
$\beta_p$	= back flow ratio at partition plate ( $=u'_p/u$ )
$\gamma$	= open area ratio of perforated plate
$\delta$	= thickness of partition plate
$\delta_o$	= thickness of perforated plate which composes the combined partition plate shown in Figure 2(b)
$\epsilon$	= ratio of volume of liquid to volume of horizontal stirred vessel ( $=V_1/V$ )
$\theta$	= time
$\theta_M$	= time for sufficient mixing
$\theta_T$	= mean residence time of liquid ( $=V_1/u$ )
$\tau$	= relaxation time of mixing
$\phi$	= dimensionless time ( $=\theta/\theta_T$ )
$\phi_{max}$	= dimensionless time when $E(\phi)$ has its maximum value
$\psi$	= dimensionless time ( $=\theta/\theta_M$ )

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